

Estimation of Expenditure Patterns in China ---based on AIDADS demand system

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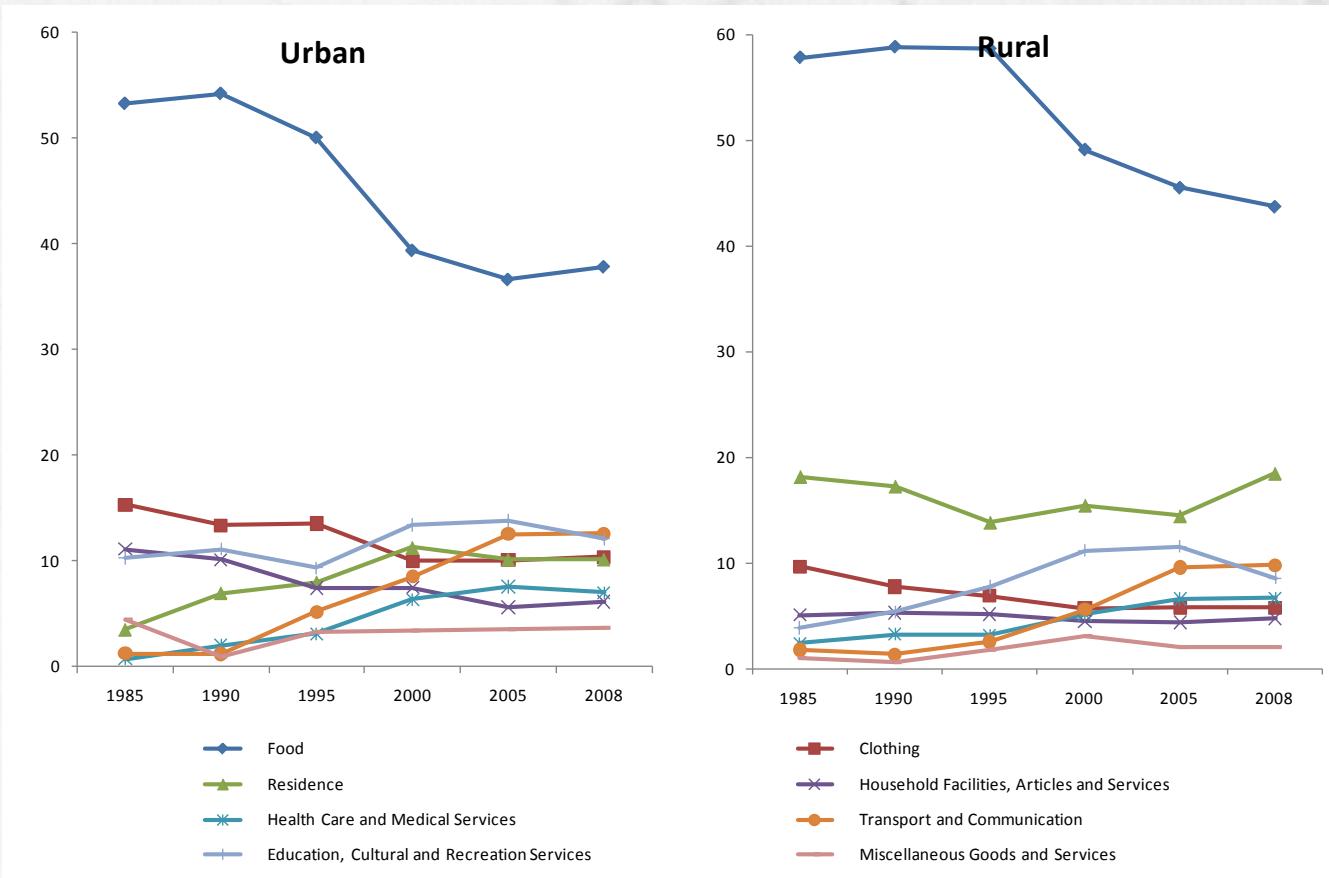
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Motivation

- structure of expenditure has changed dramatically



Motivation

- Using international cross section data / national aggregate data
- One of the world's largest countries, with high income inequality

AIDADS demand system

- AIDADS --An Implicitly Directly Additive Demand System
- LES/ELES, CDE, CD, AIDS/QUAIDS, AIDADS
- Yu et al. (2000) compared three different demand specifications (LES, CD and AIDADS)
- Cranfield et al. (2003) assesses the ability of five structural demand systems to predict demand

AIDADS

$$\min \sum_i^n p_i x_i$$

s.t

$$\sum_{i=1}^n \left(\mu_i \ln \left(\frac{x_i - \gamma_i}{A e^u} \right) \right) = 1$$

$$\mu_i = \frac{\alpha_i + \beta_i e^u}{1 + e^u}$$

$$\sum_{i=1}^n \alpha_i = \sum_{i=1}^n \beta_i = 1$$

$$0 \leq \alpha_i, \beta_i \leq 1$$



$$x_i = \gamma_i + \frac{\alpha_i + \beta_i e^u}{1 + e^u} \frac{1}{p_i} \left(y - \sum_{i=1}^n p_i \gamma_i \right)$$

$$x_i = \gamma_i + \frac{\mu_i}{p_i} \left(y - \sum_{i=1}^n p_i \gamma_i \right)$$

LES

- Follow the Maximum Likelihood estimation used in Cranfield et al.(2002)

$$\min \sum_i^{n-1} r_{ii}^2$$

s.t

$$T^{-1} \sum_{t=1}^T v_{it} v_{jt} = \sum_k^{n-1} r_{ki} r_{kj}, \quad \forall i \neq n, j \neq n, r_{kl} = 0 \text{ for all } k > l$$

$$v_{it} = s_{it} - \hat{s}_{it}$$

$$\hat{s}_{it} = \frac{p_{it}\gamma_i}{y_t} + \frac{1}{y_t} \left(\frac{\alpha_i + \beta_i e^{u_t}}{1 + e^{u_t}} \right) \left(y_t - \sum_{i=1}^n p_{it}\gamma_i \right)$$

Data Description

- ***China Household Income Project (CHIP)-2002.***
 - 6835 urban households samples from 12 provinces, including 3 eastern, 3 central and 3 western provinces of China.
 - Eight broad expenditure categories (food, clothes, home equipment, facilities and services, Health and medical expenditure, transportation and communication, entertainment, education and culture services, housing and the related and miscellaneous goods and services.)

Data



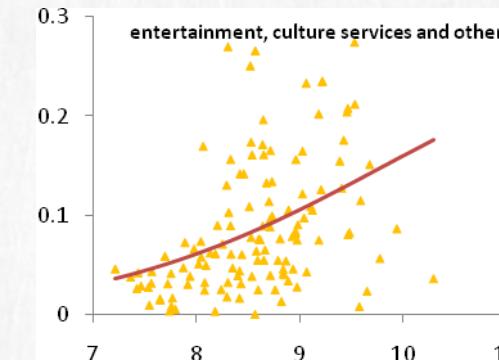
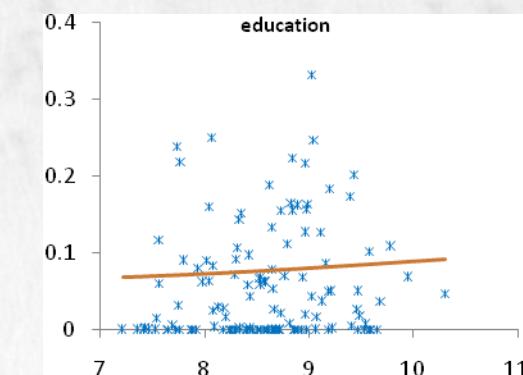
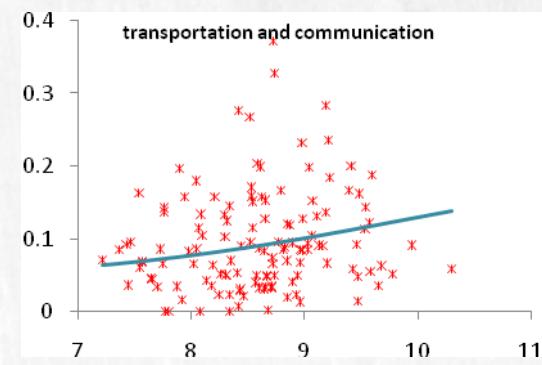
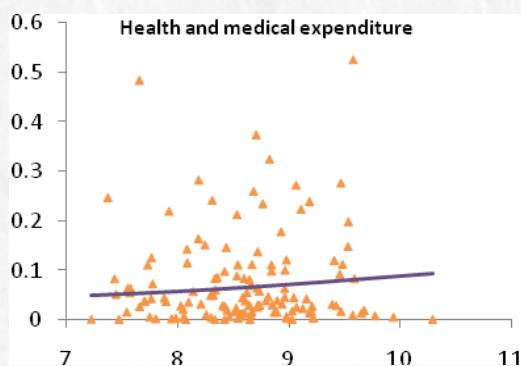
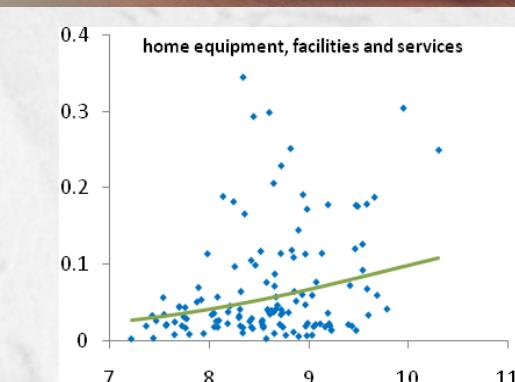
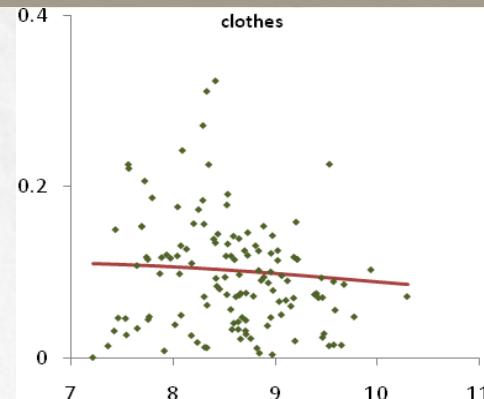
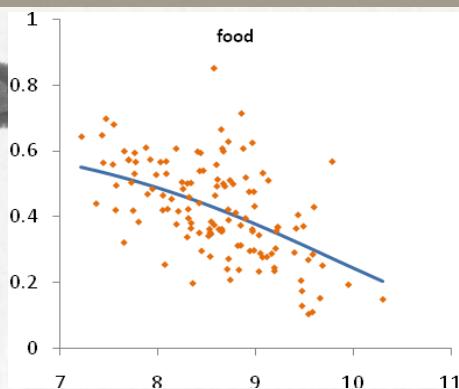
| | consumptive expenditure (yuan) | food | clothes | home equipment, facilities and services | Health and medical expenditure | transportation and communication | education | housing and the related | entertainment, culture services and others |
|--------|--------------------------------|-------|---------|---|--------------------------------|----------------------------------|-----------|-------------------------|--|
| mean | 6,279 | 0.425 | 0.102 | 0.056 | 0.067 | 0.092 | 0.133 | 0.095 | 0.030 |
| st.dev | 4,479 | 0.139 | 0.068 | 0.065 | 0.089 | 0.068 | 0.122 | 0.085 | 0.034 |
| max | 70,638 | 1.000 | 0.615 | 0.566 | 0.809 | 0.829 | 0.847 | 0.853 | 0.692 |
| min | 395 | 0.023 | - | - | - | - | - | - | - |

AIDADS estimation

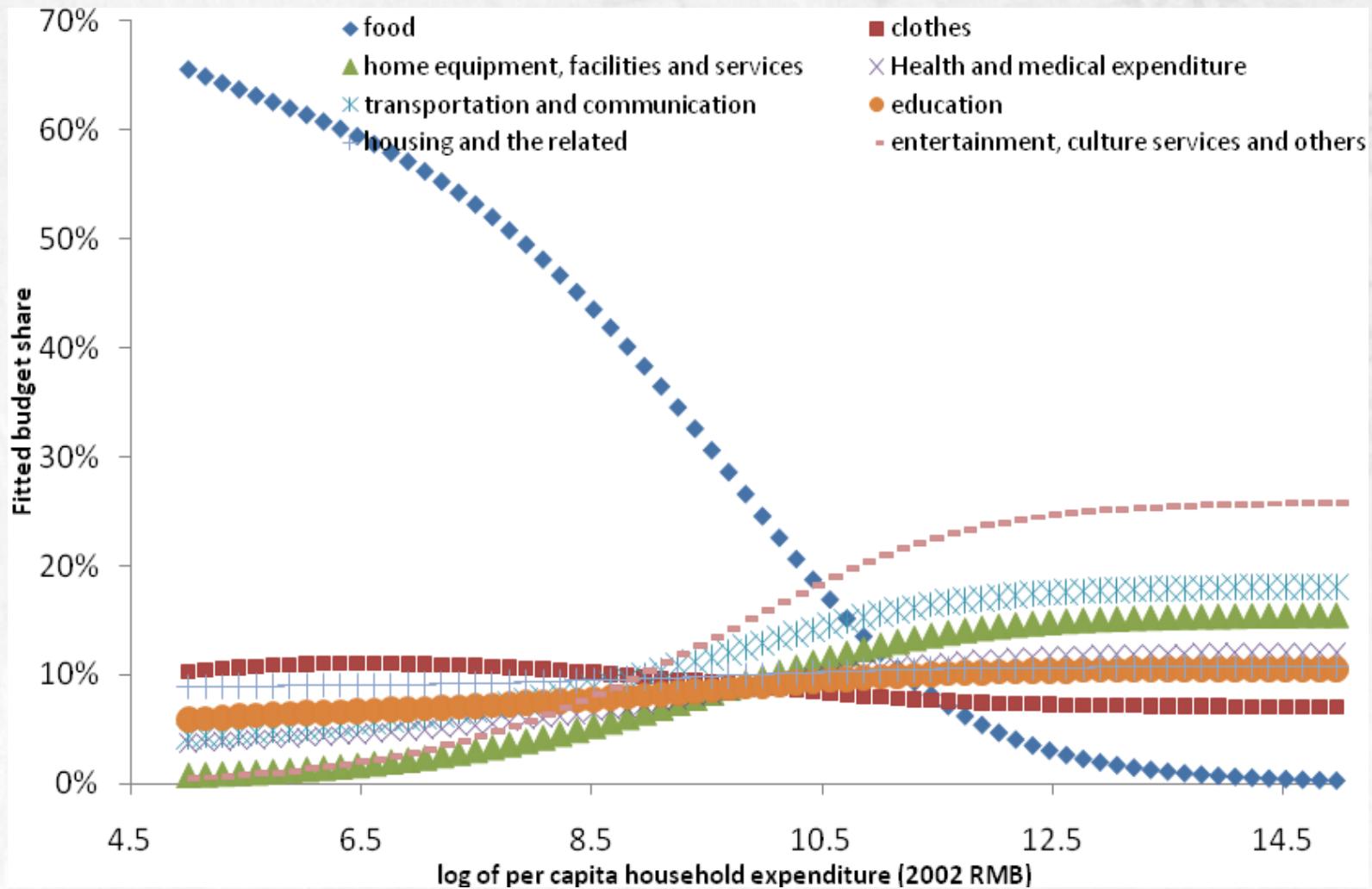


| | food | clothes | home equipment, facilities and services | Health and medical expenditure | transportation and communicatio n | education | housing and the related | entertainment, culture services and others |
|----------|--------|---------|---|--------------------------------------|--|-----------|-------------------------------|---|
| α | 0.635 | 0.117 | 0.006 | 0.041 | 0.047 | 0.065 | 0.089 | 0.000 |
| β | 0.000 | 0.071 | 0.156 | 0.121 | 0.182 | 0.105 | 0.108 | 0.258 |
| γ | 15.626 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1.500 | 0.000 |
| η | 0.714 | 0.918 | 1.472 | 1.216 | 1.268 | 1.097 | 1.036 | 1.528 |

Observed and fitted budget share



Fitted AIDADS budget share



Expenditure Elasticities

| | food | clothes | home equipment, facilities and services | Health and medical expenditure | transportation and communication | education | housing and the related | entertainment, culture services and others |
|-------------------------|-------|---------|---|--------------------------------|----------------------------------|-----------|-------------------------|--|
| National Average | 0.714 | 0.918 | 1.472 | 1.216 | 1.268 | 1.097 | 1.036 | 1.528 |
| Beijing | 0.618 | 0.901 | 1.418 | 1.216 | 1.260 | 1.102 | 1.039 | 1.456 |
| Tianjin | 0.685 | 0.912 | 1.455 | 1.217 | 1.267 | 1.100 | 1.037 | 1.504 |
| Hebei | 0.740 | 0.924 | 1.488 | 1.214 | 1.267 | 1.095 | 1.034 | 1.551 |
| Shanxi | 0.751 | 0.926 | 1.495 | 1.213 | 1.266 | 1.094 | 1.033 | 1.561 |
| Inner Mongolia | 0.746 | 0.925 | 1.492 | 1.213 | 1.267 | 1.094 | 1.034 | 1.557 |
| Liaoning | 0.733 | 0.922 | 1.483 | 1.215 | 1.267 | 1.096 | 1.035 | 1.544 |
| Jilin | 0.743 | 0.924 | 1.490 | 1.214 | 1.267 | 1.094 | 1.034 | 1.554 |
| Heilongjiang | 0.758 | 0.928 | 1.499 | 1.212 | 1.265 | 1.093 | 1.033 | 1.569 |
| Shanghai | 0.615 | 0.901 | 1.416 | 1.215 | 1.260 | 1.103 | 1.039 | 1.453 |
| Jiangsu | 0.714 | 0.918 | 1.472 | 1.216 | 1.268 | 1.097 | 1.036 | 1.527 |
| Zhejiang | 0.651 | 0.906 | 1.435 | 1.217 | 1.264 | 1.101 | 1.038 | 1.478 |
| Anhui | 0.750 | 0.926 | 1.494 | 1.213 | 1.266 | 1.094 | 1.033 | 1.560 |
| Fujian | 0.699 | 0.915 | 1.463 | 1.217 | 1.267 | 1.099 | 1.036 | 1.515 |
| Jiangxi | 0.756 | 0.928 | 1.498 | 1.212 | 1.266 | 1.093 | 1.033 | 1.566 |
| Shandong | 0.726 | 0.920 | 1.479 | 1.215 | 1.267 | 1.096 | 1.035 | 1.538 |
| Henan | 0.757 | 0.928 | 1.498 | 1.212 | 1.266 | 1.093 | 1.033 | 1.567 |
| Hubei | 0.725 | 0.920 | 1.479 | 1.215 | 1.267 | 1.096 | 1.035 | 1.537 |
| Hunan | 0.726 | 0.921 | 1.479 | 1.215 | 1.267 | 1.096 | 1.035 | 1.538 |
| Guangdong | 0.645 | 0.905 | 1.432 | 1.217 | 1.263 | 1.102 | 1.039 | 1.474 |
| Guangxi | 0.731 | 0.922 | 1.482 | 1.215 | 1.267 | 1.096 | 1.035 | 1.542 |
| Hainan | 0.730 | 0.921 | 1.481 | 1.215 | 1.267 | 1.096 | 1.035 | 1.541 |
| Chongqing | 0.706 | 0.916 | 1.467 | 1.217 | 1.267 | 1.098 | 1.036 | 1.520 |
| Sichuan | 0.731 | 0.922 | 1.482 | 1.215 | 1.267 | 1.096 | 1.035 | 1.542 |
| Guizhou | 0.754 | 0.927 | 1.497 | 1.212 | 1.266 | 1.093 | 1.033 | 1.564 |
| Yunnan | 0.720 | 0.919 | 1.475 | 1.216 | 1.267 | 1.097 | 1.035 | 1.532 |
| Tibet | 0.691 | 0.913 | 1.458 | 1.217 | 1.267 | 1.099 | 1.037 | 1.508 |
| Shaanxi | 0.732 | 0.922 | 1.483 | 1.215 | 1.267 | 1.096 | 1.035 | 1.543 |
| Gansu | 0.741 | 0.924 | 1.488 | 1.214 | 1.267 | 1.095 | 1.034 | 1.551 |
| Qinghai | 0.741 | 0.924 | 1.489 | 1.214 | 1.267 | 1.095 | 1.034 | 1.552 |
| Ningxia | 0.739 | 0.924 | 1.487 | 1.214 | 1.267 | 1.095 | 1.034 | 1.550 |
| Xinjiang | 0.725 | 0.920 | 1.478 | 1.215 | 1.267 | 1.096 | 1.035 | 1.537 |



Thanks!